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The Effects of NaCl, KCl, Mg<sup>++</sup>, Ca<sup>++</sup>, SO<sub>4</sub><sup>=</sup>, and of Boric Acid with Special Reference to Sea Water A. Distèche and S. Distèche



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# The Effect of Pressure on the Dissociation of Carbonic Acid from Measurements with Buffered Glass Electrode Cells

# The Effects of NaCl, KCl, Mg<sup>++</sup>, Ca<sup>++</sup>, SO<sub>4</sub><sup>=</sup>, and of Boric Acid with Special Reference to Sea Water

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### ABSTRACT

The effect of pressure on the dissociation of carbonic acid has been investigated over a wide range of pH (paH 5.1-9.6) and ionic strength (0-1.0) in NaCl and KCl, using junctionless glass electrode cell measurements. At 22°C,  $\Delta V_1^{\circ} = -25.4 \text{ cm}^3 \text{ mole}^{-1}$  and  $-25.6 \text{ cm}^3 \text{ mole}^{-1}$  for the first and second ionization steps, respectively. The directly measured pmH or pcH shifts induced by pressure in sea water between paH<sub>1</sub> 5.1 and 9.1 are explained by the enhanced dissociation of H<sub>2</sub>CO<sub>3</sub>, HCO<sub>3</sub><sup>-</sup>, CaCO<sub>3</sub>, and MgCO<sub>3</sub>, the effect of SO<sub>4</sub><sup>=</sup> and the interference of boric acid ( $\Delta V_1^{\circ} = -32.1 \text{ cm}^3 \text{ mole}^{-1}$ ). Values of the ionization functions  $k'_{(1)} = [\text{H}^+][\text{HR}^-]/[\text{H}_2\text{R}]$  and  $k'_{(2)} = [\text{H}^+][\text{R}^=]/[\text{HR}^-]$  of carbonic acid, valid in natural seawater, have been determined at 22°C, at 1 atm and at 1000 bars together with the apparent dissociation constants ( $pK''_{(1)}$  and  $pK''_{(2)}$  used in oceanography to calculate  $[\text{CO}_3^=]_{\text{total}}$ ,  $[\text{HCO}_3^-]_{\text{total}}$  from *in situ* paH values. Corrections are given for different types of reference half-cells, and an approach toward the absolute values of  $pk_{(1)}$  and  $pk_{(2)}$  in sea water is indicated.

The effect of pressure (p) on the dissociation constant (K) of a weak electrolyte (HR) is related to the corresponding volume change  $(\Delta V)$  for the ionization reaction  $HR \rightleftharpoons H^+ + R^-$  by the equation

$$\left(\frac{\partial \ln K}{\partial p}\right)_{m,T} = \frac{-\Delta V}{RT}$$
 [1]

Ag

Data are available for  $\Delta V_1^{0}$  at atmospheric pressure, zero salt concentration, and zero weak electrolyte concentration for carbonic acid calculated from density and  $SO_4^{=}$  ions and boric acid is investigated to interpret the data obtained with natural sea water samples (4) and from direct in situ determinations (5, 6).

#### Theoretical

The theory underlying the determination of dissociation constants as a function of pressure has been discussed in previous papers (3, 4).

The buffered cell used for the present determinations is of the type:

- AgCl	Ref. compartment HCl $(0.01)$ MCl $(m_3 - 0.01)$	glass	$\operatorname{K} \operatorname{compartment}_{\operatorname{HR}(m_1) + \operatorname{MR}(m_2)}$ MCl $(m_3)$	AgCl – Ag
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where M represents Na or K.

measurements, conductivity, and glass electrode determinations:

	25°C	ity, 25°C	trode, 22°C
Reaction	$-\Delta V_p^{\circ}$ (p = 1 atm) cm <sup>3</sup> mole <sup>-1</sup>	$-\Delta V_p^{\circ}$ $(p = 1 \text{ atm})$ $\text{cm}^3 \text{ mole}^{-1}$	$-\Delta V_p^{\circ}$ (p = 1 atm) cm <sup>3</sup> mole <sup>-1</sup>
$H_2CO_3 \rightarrow HCO_{3^-} + H^+$	29.0 (1)	26.5 (2)	26.6 (3) (unbuff- ered cell) 25.5 (3) (buff- ered cell) 25.4 (this paper; buffered cell)
$HCO_{3^-} \rightarrow CO_{3^=} + H^+$	27.8 (1)	-	25.6 (this paper;

The  $\Delta V_1^{0}$  values from glass electrode measurements published in our earlier papers (3, 4) were obtained by extrapolation of  $\Delta V_1$  to zero KCl concentration over a limited ionic strength range (0-0.1).

In view of the interest in precise knowledge of the effect of pressure on the dissociation of carbonic acid for oceanographic work, the present paper deals with the determination between 1 and 1000 atm of the dissociation constants  $K_{(1)}$  and  $K_{(2)}$  and the ionization functions  $k_{(1)}$ ,  $k_{(2)}$  ( $k_{(1)} = [H^+][HCO_3^-]/[CO_2]$ ,  $k_{(2)} = [H^+][CO_3^-]/[ICO_3^-]$ ) in presence of NaCl or KCl, over a wide ionic strength range (0-0.8), at various buffer ratios (paH 5.1-9.6). The effect of Ca<sup>++</sup>, Mg<sup>++</sup>,

The emf (E) at pressure 1, or p, is expressed by:  $E_{1,p} \mathbf{F}/2.3 RT = \log (m_{\mathrm{H}+})^{\mathrm{ref}}_{1,p} - \log (m_{\mathrm{H}+})^{\mathrm{x}}_{1,p}$ 

$$+ 2 \log \frac{(\gamma_{\rm HCl})^{\rm ref}_{1,p}}{(\gamma_{\rm HCl})^{\rm x_1} p} \quad [2]$$

For an acid HR of the strength of carbonic acid log  $K^m = \log (m_{\rm H} + m_1/m_2) + 2 \log \gamma_A$ ; 2 log  $\gamma_A = \log (\gamma_{\rm H} + \gamma_{\rm R} - /\gamma_{\rm HR})$ ;  $m_{\rm H} + m_1/m_2 = k^m$  and:

$$(E_1 - E_p)\mathbf{F}/2.3 RT = \log \frac{K^m_p}{K^m_1} + 2\log \frac{\gamma_{A_1}}{\gamma_{A_p}} + 2\log \frac{(\gamma_{HCl})^{\operatorname{ref}_1}}{(\gamma_{HCl})^{\operatorname{ref}_p}} - 2\log \frac{(\gamma_{HCl})^{x_1}}{(\gamma_{HCl})^{x_p}}$$
[3]

The terms in  $\gamma_{\text{HCl}}$  cancel each other at infinite dilution of the weak electrolyte, but if  $m_1$  and  $m_2$  are small and if the salt effect of the weak acid is small, cancellation practically occurs for finite values of  $m_1$ and  $m_2$ .

Equation [3] then simplifies to

$$(E_1 - E_p) \mathbf{F}/2.3 RT = \log \frac{K^m_p}{K^m_1} + 2\log \frac{\gamma_{A_1}}{\gamma_{A_p}} = \log \frac{k'^m_p}{k'^m_1}$$
[4]

the primes indicating that k' is only known approximately because of the former assumptions.

In the case of carbonic acid, extrapolation of  $(E_1 - E_p)$  **F**/2.3 *RT* as a function of  $\sqrt{\mu}$  leads easily to log  $K^m_p/K^{m_1}$  and a double extrapolation first to zero weak acid concentrations at a given  $\mu$ , and then to zero KCl or NaCl concentration, is not required.

It can be shown (7) that  $\Delta V_1 = 1.016 \ge (E_1 - E_{1000})$ if  $\Delta V_1$  is expressed in cm<sup>3</sup> mole<sup>-1</sup>, *E* in millivolts, *p* in kg. cm<sup>-2</sup>.  $E_{1000}$  is measured on the tangent of  $E_1 - E_p$ = f(p) drawn through p = 1 atm. For carbonic acid,  $E_1 - E_p = \Delta E_p$  is a linear function of *p* up to 1000 kg. cm<sup>-2</sup>, so that  $E_{1000}$  corresponds to the emf effectively measured at 1000 kg. cm<sup>-2</sup>.

Concentrations (m) and activity coefficients  $(\gamma)$  are given on the molal scale (mole per kg of pure solvent) in Eq. [1]-[4].

If the concentrations are expressed on the molar scale (mole per liter solution, c) the following classical equations ([5]-[10]) can be used to relate c, m, the corresponding activity coefficients, y and  $\gamma$ , the density (d) of the solution and of pure water ( $d_o$ ),  $M_i$  the molecular weight of solute *i*. the dissociation constants and ionization functions  $K^c$ ,  $k^c$ ,  $K^m$ ,  $k^m$ 

$$m_i = c_i / (d - \Sigma c_i M_i / 1000)$$
 [5]

$$c_i = m_i d / (1 + \Sigma m_i M_i / 1000)$$
 [5']

$$\gamma = \eta \left[ \left( d - \Sigma c_{i} M_{i} / 1000 \right) / d_{2} \right]$$
 [6]

$$m_{\gamma}d_o = cy$$
 [7]

$$K^m = K^c/d_o; \ k^m = k^c(1 + \Sigma m_i M_i / 1000) / d$$
 [8]

 $\log K^{m}_{p}/K^{m}_{1} = \log K^{c}_{p}/K^{c}_{1} - \log d_{op}/d_{o1}$ [9]

$$\log k^{m}_{p}/k^{m}_{1} = \log k^{c}_{p}/k^{c}_{1} - \log d_{p}/d_{1}$$
 [9']

Combining [7] and [2] gives

$$\frac{(m\gamma)^{\operatorname{ref}_{1,p}}}{(m\gamma)^{\operatorname{x}_{1,p}}} = \frac{(cy)^{\operatorname{ref}_{1,p}}}{(cy)^{\operatorname{x}_{1,p}}}$$
[10]

If the activity coefficients can be made to cancel in both ref and x compartments of the glass electrode,  $(E_1 - E_p)\mathbf{F}/2.3 \text{ RT}$  will be equal to  $\log k'^m_p/k'^m_1$  and extrapolate to  $\log K^m_p/K^m_1$  as a function of  $\mu$  (Eq. [4]) whatever the concentration scale used.

In aqueous solutions  $d_p/d_1 = d_{op}/d_{o1} = 1.04$  at 1000 atm, log  $d_{1000}/d_1 = 0.017$ , and it is thus easy to use  $(E_1 - E_{1000})$  to calculate the ratios of the dissociation constants and ionization functions either on the c or the *m* scale.

When the absolute values of  $k'^{m_1}$ ,  $k'^{c_1}$  are required, Eq. [5], [5'], and [6] can be used to calculate either ionization function from the results obtained on the c or the *m* scale, respectively.

In practice, if the highest precision is not required,  $c \simeq m$  at 0.1M. At concentrations where the correction to calculate m from c is more important, the densities in the x and ref compartments of the glass electrode are nearly equal when the buffer concentration is small compared with the NaCl or KCl concentrations, and only  $m_{\rm H}$  + needs be computed in the reference solution, since  $m_{\rm Cl}$ - $^{\rm x} = m_{\rm Cl}$ - $^{\rm ref}$ .

In the present paper, concentrations referring to the gross composition of the solutions are indicated on the molar scale, and to simplify the symbol M referring to molarity is omitted (0.5 NaCl means 0.5M NaCl). The hydrogen ion stoichiometric concentration [H<sup>+</sup>] is represented by  $pcH = -\log [H^+]$  on the *c*-scale and pmH on the *m*-scale, the hydrogen ion activity  $a_{H^+}$  by  $paH = -\log a_{H^+}$  and if the distinction between pcH, pmH, paH is irrelevant, the symbol pH is used; subscripts p, 1, 1000 indicate pressure p, 1 atm, 1000 kg. cm<sup>-2</sup> (ex. :  $pmH_1$ ,  $pmH_{1000}$ );  $\Delta E_{1000} = E_1 - E_{1000}$  in millivolts (mv).

#### Experimental

The equipment described in 1962 (7) is used. It is important in the experiments involving equilibration with either pure  $CO_2$  or mixtures of  $CO_2$  and nitrogen to saturate the silicone oil used in the glass electrode cell and to fill the cell with pipettes containing a controlled gas phase (3).

The glass electrode is made from Corning 015 glass, when no sodium error is to be expected. A commercial electrode, E.I.L.<sup>1</sup>  $n^{\circ}$  18331 unsensitive toward Na<sup>+</sup> at alkaline pH is used whenever necessary.

Corrections for asymmetry potential shift with pressure is made as described earlier (3, 4, 7). When both cell compartments contain the same solution  $\Delta E_{1000}$ is generally between 0 and  $\pm 1.0$  mv. Higher values indicate defective Ag-AgCl electrodes.

Highest grade reagents (Merck) and air-free bidistilled water (Pyrex) are used.

#### Results

First ionization function and first dissociation constant of carbonic acid in bicarbonate buffer in presence of NaCl or KCl, at p = 1 atm and p = 1000 kg.  $cm^{-2}$ .—Figure 1 shows  $\Delta E_{1000}$  in mv as a function of  $\sqrt{\mu}$  for various bicarbonate buffers at different buffer ratios, in presence of NaCl or KCl. Extrapolation to zero ionic strength gives 25.0 mv corresponding to  $-\Delta V_{1^0} = 25.4$  cm<sup>3</sup> mole<sup>-1</sup>, in agreement with our previous experiments (4).

Figure 2 gives the ionization function  $pk'^{c}_{(1)} = -\log k'^{c}_{(1)}$  and  $pK'^{c}_{(1)} = -\log K'^{c}_{(1)} = pk'^{c}_{(1)} + \frac{1.01\sqrt{\mu}}{1+\sqrt{\mu}}$ 

as a function of  $\mu$  at p = 1 atm and  $pK^{c}_{(1)p} + \log d_p/d_1$  at p = 1000 kg. cm<sup>-2</sup> (log  $d_p/d_1 = 0.017$ ). The absolute values of  $pK^{c}_{(1)}$  (6.38) and  $pk'^{c}_{(1)}$  are

The absolute values of  $pK^{c}_{(1)}$  (6.38) and  $pK'^{c}_{(1)}$  are in good agreement with the data of Harned and Davis (8) and of Harned and Bonner (9) ( $pK^{m}_{(1)} = 6.3809$ at 20° and 6.3519 at 25°C).

The concentration ratios  $[\text{HCO}_3^-]/[\text{CO}_2]$  are computed from the equations of these authors and the same extrapolation function is found to fit our results and theirs. The 2 log  $(y_{\text{HCI}})^{\text{ref}}/(y_{\text{HCI}})^{\text{x}}$  term in Eq. [1] (c scale) is calculated from the values of  $\gamma_{\text{HCI}}$ in NaCl and KCl taken from Harned and Owen (10). It is assumed that  $\gamma_{\text{HCI}}$  in the x compartment is only affected by the ionic strength, and the ratio of the activity coefficients is also supposed to be valid on the molar scale. At  $\mu \ge 0.5$ ,  $\gamma_{\text{HCI}}$  practically cancels in both compartments.

At  $\mu = 0.75$ ,  $pk'^{m}{}_{(1)} = pk'^{c}{}_{(1)} - 0.007 = 5.995$ . The correction is -0.005, -0.0057, -0.0065, -0.0073,

<sup>1</sup> Electronic Instruments Limited, Richmond, Surrey, England.



Fig. 1. Glass electrode emf shifts at 22°C produced by pressure (1000 kg.cm<sup>-2</sup>), in bicarbonate buffers, at different buffer ratios, as a function of  $\sqrt{\mu}$ , in NaCl, KCl, in presence of Mg<sup>++</sup>, Ca<sup>++</sup>, SO<sub>4</sub><sup>=</sup> ions, and in sea water.

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Fig. 2. First ionization function  $(k'c_{(1)})$  of carbonic acid and as a function of  $\mu$  at atm pressure and 1000 kg.cm<sup>-2</sup> in NaCl and KCl at 22°C. Effect of MgSO<sub>4</sub> + MgCl<sub>2</sub>.

-0.0081, -0.009 at  $\mu$ 0.5, 0.6, 0.7, 0.8, 0.9, 1.0, respectively (calculated from the density of NaCl solutions), and at  $\mu = 0$ , it is equal to -0.001.

Second ionization function and second ionization constant of carbonic acid in carbonate buffer in presence of NaCl or KCl, at p = 1 atm and p = 1000kg. cm<sup>-2</sup>.—Figure 3 gives  $\Delta E_{1000}$  in mv, as a function of  $\sqrt{\mu}$  for carbonate buffer in presence of NaCl or KCl.

Extrapolation to zero ionic strength gives 25.1 mv or  $-\Delta V_1^{\circ} = 25.6$  cm<sup>3</sup> mole<sup>-1</sup>, which is practically the same result obtained in bicarbonate buffers. The value calculated by Owen and Brinkley (1) from density determinations is 27.8 cm<sup>3</sup> mole<sup>-1</sup>.

Figure 4 shows the ionization function  $pk'^{c}{}_{(2)}$  as a function of  $\sqrt{\mu}$  at p = 1 atm,  $pk'^{c}{}_{(2)p} + \log d_p/d_1$  at p = 1000 kg. cm<sup>-2</sup>; the results in 0.5 and 0.8 NaCl do not depend on the buffer ratio and are identical either with NaHCO<sub>3</sub> 0.08 + Na<sub>2</sub>CO<sub>3</sub> 0.01 or with NaHCO<sub>3</sub> 0.025 + Na<sub>2</sub>CO<sub>3</sub> 0.025.  $pK^{c}{}_{(2)} = 10.37$  corresponds to the values published by Harned and Scholes (11)  $(pK^{m}{}_{(2)} = 10.377$  at 20°C, 10.329 at 25°C) who extrapolate their data between  $\mu = 0.15$  and 0.

At  $\mu = 0.75$ ,  $pk'^{m}_{(2)1} = 9.60 - 0.007$  in NaCl.

Effect of buffer ratio on the ionization of carbonic acid at 1000 kg.  $cm^{-2}$  in NaCl and KCl solutions.— Figures 1 and 3 show that, at a given buffer ratio,  $\Delta E_{1000}$  extrapolates linearly to the same value at  $\mu = 0$ , and that a change in the buffer concentration has the



Fig. 3. Glass electrode emf shifts at 22°C, produced by pressure (1000 kg.cm<sup>-2</sup>) in carbonate buffers, at different buffer ratios, as a function of  $\sqrt{\mu_{\nu}}$  in NaCl or KCl, in presence of Mg<sup>++</sup>, Ca<sup>++</sup>, SO<sub>4</sub><sup>=</sup>, and in sea water.



Fig. 4. Second ionization function  $(k'^{c}_{(2)})$  of carbonic acid as a function of  $\sqrt{\mu}$  at atm pressure and 1000 kg.cm<sup>-2</sup> in NaCl and KCl at 22°C. Sulfate effect of 0.030 MgSO<sub>4</sub> (+0.026 MgCl<sub>2</sub>).

same effect as the corresponding  $\mu$  change produced by an increase of the NaCl or KCl concentration. It is therefore easy to obtain a graphical estimate of  $\Delta E_{1000}$ at a chosen ionic strength, even from isolated values measured at another ionic strength.

Curves 1 and 1' from Fig. 5 give  $\Delta E_{1000}$  at  $\mu = 0.75$  (ionic strength of sea water at  $Cl\%_0 = 20.0$ ) as a function of  $pmH_1$ , in NaCl and KCl. The emf shifts depend only slightly on the total CO<sub>2</sub> concentration in the range investigated ([HCO<sub>3</sub>-] + [CO<sub>3</sub>-] between 0.09 and 0.0025; arrows indicate the values at 0.0025 in Fig. 5).

The reason for the difference between the results in NaCl and KCl at  $pmH_1 \ge 8.5$  is, we believe to be correlated with the fact that, at 1 atm, the curves giving  $pk'_{(2)}$  as a function of  $\sqrt{\mu}$  (Fig. 3) demonstrate the greater tendency for carbonate ions to associate with Na than with K. Ion pairs like  $Na^+ - CO_3^=$  or  $Na^+$ NaCO3<sup>-</sup> will dissociate under pressure, and free  $CO_3$  = ions, hitherto masked for the carbonic acid equilibrium, will modify the buffer ratio, so that the pmH shift induced by pressure can be expected to be smaller than in a medium where association is less important or inexistent. We will see that magnesium and calcium ions which have a much larger tendency to form ion pairs with  $CO_3^{=}$  than sodium ions also have a much larger lowering effect on the emf changes produced by pressure in carbonate buffers.

Since  $K^+$  or Na<sup>+</sup> may also form ions pairs with  $HCO_3^-$ , a complete analysis of curves 1 and 1' appears to be far from easy and would require the knowledge of  $pk'_{(1)(2)}$  and  $\Delta pk'_{(1)(2)}/\Delta p$  in absence of any ionic association; the dissociation constants of  $NaCO_3^-$  and  $NaHCO_3$  would have to be taken into account and also the equilibrium  $2HCO_3^- \rightleftharpoons CO_3^- + H_2CO_3$ , which is displaced when  $CO_3^-$  or  $HCO_3^-$  is released in the solution. Besides the salt effect of NaCl or KCl would have to be known.

There is however no difficulty in considering that in the ionization functions  $k'_{(1)}$  and  $k'_{(2)}$ , determined at atmospheric pressure or at 1000 kg. cm<sup>-2</sup>, [CO<sub>3</sub>=] and [HCO<sub>3</sub>-] refer to the total concentration of CO<sub>3</sub>= of HCO<sub>3</sub>-, ions present either as free ions or forming ion pairs with Na or K.

In the  $pmH_1$  interval 8.5-9.5 the thus defined  $pk'_{(2)1000}$  can be measured without ambiguity from curves 1 and 1' of Fig. 5 since  $\Delta E_{1000}$  is constant. The buffer ratio and the term 2 log  $\gamma_{A1}/\gamma_{Ap}$  in Eq. [3] are constant, the mean activity coefficient being referred to the total concentrations of free and masked ions. Log  $k'^m_{(2)1000}/k'^m_{(2)1}$  is therefore equal to 0.315 ( $\Delta E_{1000} = 19.0 \text{ mv}$ ) and 0.350 ( $\Delta E_{1000} = 20.8 \text{ mv}$ ) in NaCl and KCl, respectively.



Fig. 5. Glass electrode emf shifts at 22°C produced by pressure (1000 kg.cm<sup>-2</sup>) in bicarbonate, carbonate buffers, and sea water at  $\mu = 0.75$ , as a function of pmH =  $-\log m_{\rm H}$  measured at atm pressure. Curve 1, NaHCO<sub>3</sub>, Na<sub>2</sub>CO<sub>3</sub>, CO<sub>2</sub> ( $[HCO_3^-] + [CO_3^-]$ 0.05 — 0.09 and 0.0025 (arrow) in 0.5 NaCl. Curve 1', KHCO<sub>3</sub>,  $K_2CO_3$ ,  $CO_2$  ([HCO<sub>3</sub><sup>-</sup>] + [CO<sub>3</sub><sup>=</sup>] 0.05 - 0.09) in 0.5 KCl. Curve 2, NaHCO<sub>3</sub>, Na<sub>2</sub>CO<sub>3</sub>, CO<sub>2</sub> ([HCO<sub>3</sub><sup>-</sup>] + [CO<sub>3</sub><sup>=</sup>] 0.05 -0.09) in 0.5 NaCl; effect of Na<sub>2</sub>SO<sub>4</sub> (0.030). Curve 3, NaHCO<sub>3</sub>, Na<sub>2</sub>CO<sub>3</sub>, CO<sub>2</sub> ([HCO<sub>3</sub><sup>-</sup>] + [CO<sub>3</sub><sup>=</sup>] 0.05 - 0.09) in 0.5 NaCl; effect of MgSO<sub>4</sub> (0.030), MgCl<sub>2</sub> (0.026), CaCl<sub>2</sub> (0.01) (Precipitates are obtained at pH > 8.0). Arrows indicate results for [HCO<sub>3</sub><sup>-</sup>]  $[CO_3^{=}] = 0.0025$  (see also curve segments 6). Curve 3', NaHCO<sub>3</sub>, Na<sub>2</sub>CO<sub>3</sub>, CO<sub>2</sub> ([HCO<sub>3</sub><sup>-</sup>] +  $[CO_3^{-}]$  0.05 - 0.09) in 0.5 NaCl;  $SO_4$  = effect of MgSO<sub>4</sub> (0.030). Curve 4, NaHCO<sub>3</sub>,  $Na_2CO_3$ ,  $CO_2$  ([HCO<sub>3</sub><sup>-</sup>] + [CO<sub>3</sub><sup>=</sup>] 0.05 - 0.09 and 0.025 (arrows); effect of MgCl<sub>2</sub> (0.056). Curve 5, Natural sea water Cl  $\%_{0} \simeq 19.5$  (Atlantic), corrected at Cl $\%_{0}$  20.0 ( $\mu = 0.75$ ). Curve 5', Natural sea water; SO4 = effect. Curve 6, Artificial sea water:  $[HCO_3] + [CO_3^{=}] = 0.0025; 0.030 MgSO_4, 0.026 MgCl_2,$ 0.010 CaCl<sub>2</sub>, 0.5 NaCl (with or without boric acid in the acid range). Curve 6', Artificial sea water with boric acid  $(4.3 \ 10^{-4})$ (alkaline range). Curve 7, Effect of boric acid; smoothed difference in my between  $(E_1 - E_{1000})$  in artificial sea water without boric acid (see curves 3 and 6) and  $(E_1 - E_{1000})$  in the same with 4.3  $10^{-4}$  boric acid (see curves 6 and 6').

Inspection of curve 1 further indicates that the results at  $pmH_1 \leq 7.00$  are identical in KCl and NaCl. If one again assumes that the bicarbonate concentration corresponds to the sum of the free  $HCO_3^-$  ions and the undissociated sodium or potassium bicarbonate, log  $k'^m_{(1)1000}/k'^m_{(1)1}$  is equal to 0.359 ( $\Delta E_{1000} = 21.0 \text{ mv}$ ) at  $pmH_1$  7.0, 0.376 at  $pmH_1$  6.0, and 0.385 at  $pmH_1$  5.0. Here the term 2 log  $\gamma_{A1}/\gamma_{Ap}$  in Eq. [3] is not constant and depends on the buffer ratio.

The question that remains to be answered concerns the choice of suitable values for  $pk'_{(1)1000}$  and  $pk'_{(2)1000}$ in the  $pmH_1$  range 7.0-8.5, where the emf changes induced by pressure depend on both ionization functions.

If we consider a solution containing NaCl and NaHCO<sub>3</sub> at atmospheric pressure, its  $pmH_1 = \frac{1}{2}$   $(pk'^{m}_{(1)1} + pk'^{m}_{(2)1})$ ; at  $\mu = 0.75$ , one finds  $pmH_1 \simeq 7.8 = \frac{1}{2}$  (6.0 + 9.6) and  $[CO_2] = [CO_3=]$ . At  $pmH_1 = 7.8$ ,  $\Delta E_{1000} = 20.0$  mv, and simple considerations show that  $[CO_2]$  will remain equal to  $[CO_3=]$  if 2.3 RT/F log  $k'^{m}_{(1)1000}/k'^{m}_{(1)1}$  and 2.3 RT/F log  $k'^{m}_{(2)1000}/k'^{m}_{(2)1}$  are taken symmetric with respect to  $\Delta E_{1000} = 20.0$  mv.

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For instance, 21.0 and 19.0 mv read at  $pmH_1$  7.0 and 8.5 on curve 1 of Fig. 5. In that case the equilibrium  $2HCO_3^- \rightleftharpoons CO_3^= + H_2CO_3$  is shifted. Thus, at  $pmH_1$ = 7.8, if  $[HCO_3^-] + [CO_3^-] = 0.05, 6.10^{-5} HCO_3^-$  is formed at 1000 kg. cm<sup>-2</sup> at the expense of  $3.10^{-5} CO_2$ and  $3.10^{-5} CO_3^=$ , which corresponds to a 4% change of the initial CO<sub>2</sub> and CO<sub>3</sub><sup>=</sup> concentrations. At  $pmH_1$ 7.0 and 8.5, the change of either  $[CO_2]$  and  $[HCO_3^-]$ or  $[CO_3^=]$  and  $[HCO_3^-]$  is negligible when pressure is applied. If one could assume 2.3  $RT/F \log k'^{m}(1)1000/k'^{m}(1)1$  and 2.3  $RT/F \log k'^{m}(2)1000/k'^{m}(2)1$  to be equal to  $\Delta E_{1000}$  read on curve 1 at any  $pmH_1$  between 5.0 and 9.0, the CO<sub>2</sub>,  $HCO_3^-$ ,  $CO_3^=$  concentrations would remain constant at any pressure. This is what happens at infinite dilution where  $\Delta V^o(1)_1 = \Delta V^o(2)_1$ .

In KCl, if one neglects the slight minimum at  $pmH_1$ 7.8, 2.3 RT/F log  $k'^m_{(1)1000}/k'^m_{(1)1}$  and 2.3 RT/F log  $k'^m_{(2)1000}/k'^m_{(2)1}$  are equal within  $\pm$  0.25 mv over the range 7.0-9.0. However, this is an oversimplification since the minimum at 7.8 could be explained by the release of  $CO_3^=$  and  $HCO_3^-$  from ion pairs.  $HCO_3^$ behaves as a base at  $pmH_1 < 7.8$  and as an acid at  $pmH_1 > 7.8$ , whereas the release of  $CO_3^=$  always results in lowering the hydrogen ion concentration.

The choice of the values of  $pk'^{m}_{(1)1000}$  at  $pmH_1$  7.0 and  $pk'^{m}_{(2)1000}$  at  $pmH_1$  8.5 to be used in the  $pmH_1$ interval 7.0-8.5 remains questionable, even in KCl, but there is no other alternative unless reliable values for  $pk'^{m}_{(1)}$  and  $pk'^{m}_{(2)}$  become available in absence of any ionic association. However, at the alkaline end of the  $pmH_1$  interval 7.0-8.5,  $pk'^{m}_{(1)}$  needs not to be known with great precision to calculate [HCO<sub>3</sub><sup>-</sup>] or [CO<sub>3</sub><sup>=</sup>]. At  $pmH_1$  8.0, an error of 0.02 ( $\Delta E \simeq 1.2 \text{ mv}$ ) in  $pk'^{m}_{(1)1000}$  affects [CO<sub>2</sub>] by 2% and [HCO<sub>3</sub><sup>-</sup>] and [CO<sub>3</sub><sup>=</sup>] by only 0.1%.

The separate salt effect of NaCl on 2.3 RT/F log  $k'^{m}_{(1)1000}/k'^{m}_{(1)1}$  can be estimated at  $pmH_1 < 5.0$  since curve 1 in Fig. 5 seems to reach a plateau in the acid range and since  $\Delta E_{1000}$  is known at 0 ionic strength (25.0 mv). Thus, for the salt effect, one finds 25.0 – 22.6 = 2.4 mv. This value fits with the fact that  $2 \Delta E_{1000}$  = 23.6 mv at  $\mu = 0.75$  in a solution containing only NaCl and saturated with CO<sub>2</sub>. At  $\mu = 0$ ,  $2 \Delta E_{1000} = 26.2 \text{ mv}$  (3) and the difference 26.2 - 23.6 = 2.6 mv.

It seems reasonable to assume that the difference between  $\Delta V_{1}^{o_{1}}$  found in pure CO<sub>2</sub> solutions and in bicarbonate buffer at 0 ionic strength might be related to the existence of NaHCO<sub>3</sub> ion pairs even when the concentration of NaHCO<sub>3</sub> becomes very small. The same effect occurs in other buffer systems investigated with the glass electrode technique:  $\Delta V_{1}^{o_{1}}$  is always found to be smaller in buffers than in the corresponding pure acid (3), and the explanation given above might be general.

Finally, one will notice (Fig. 5, dotted part of curves 1 and 2) that Corning 015 electrodes display an alkaline error in presence of NaCl at 1000 kg. cm<sup>-2</sup> at  $pmH_1 > 8.25$ , although no such error can be detected even at 8.75 at atmospheric pressure.

Ionization of carbonic acid in presence of Mg<sup>++</sup>.  $Ca^{++}$ , and  $SO_4^{=}$  in NaCl solutions, at concentrations found in sea water, at 1 atm and 1000 kg.  $cm^{-2}$  and at different buffer ratios ( $\mu = 0.75$ ).—When Ca or Mg salts are added to carbonate and bicarbonate buffers, it is well known [see Garrels, Thompson, and Siever (12)] that MgCO<sub>3</sub> and CaCO<sub>3</sub> ion pairs are formed and that the trapping of  $HCO_3^-$  ions is also to be considered. The dissociation of carbonic acid can still be described by the ionization functions  $k'_{(1)}$  and  $k'_{(2)}$ where  $[CO_3^{=}]$  and  $[HCO_3^{-}]$  refer to the free carbonate and bicarbonate ions (plus those bound to Na as seen in the preceding section), but it is also useful to define apparent ionization functions  $k''_{(2)} =$ [H<sup>+</sup>]  $[CO_3^{=}]_T/[HCO_3^{-}]_T$ ,  $k''_{(1)} = [H^+] [HCO_3^{-}]_T/[CO_2]$  where  $[CO_3^{=}]_T$  and  $[HCO_3^{-}]_T$  correspond to the total amount of carbonate and bicarbonate. We will call  $k'_{(2)}$  and  $k'_{(1)}$  true ionization functions.

True and apparent ionization functions of carbonic acid in presence of  $Mg^{++}$ ,  $Ca^{++}$  and  $SO_4^{=}$ , in NaCl solutions at 1 atm ( $\mu = 0.75$ ).—Figure 6 gives the  $pmH_1$  changes (in mv) produced when  $MgCl_2$ , curve 4;  $MgCl_2 + MgSO_4$ , curve 3;  $MgCl_2 + MgSO_4 + CaCl_2$ , curve 2; Na<sub>2</sub>SO<sub>4</sub>, curve 1 are added to bicarbonate and carbonate buffers at atmospheric pressure, as a function of  $pmH_1$  measured in the solutions containing the added salts. The reference 0.01 HCl + 0.49 NaCl solution has the same salt composition as the buffer under test it is assumed that  $m_{H+} = m_{HCl}$  and that the mean activity coefficient of HCl is the same in both compartments. The added salts are tested at concentrations normally found in sea water (Cl%<sub>0</sub> = 20.0).

Effect of  $SO_4^=$  on the true ionization functions  $k'_{(1)1}$ and  $k'_{(2)1}$ .—Inspection of Fig. 6 shows that the effect of  $SO_4^=$  ions can be distinguished from the effect of Ca and Mg.

MgCl<sub>2</sub> at  $pmH_1 < 6.0$  obviously does not modify  $k'^c_{(1)1}$  which is thus the same as in pure bicarbonate solutions at the same ionic strength. The ordinate difference between curves 3 and 4 in Fig. 6 shows but little variations over the  $pmH_1$  interval considered and allows one to calculate  $pk'^c_{(1)1}$  and  $pk'^c_{(2)1}$ . Thus for the investigated buffers (MgSO<sub>4</sub> 0.030, [HCO<sub>3</sub><sup>-</sup>] + [CO<sub>3</sub><sup>-</sup>] between 0.0025 and 0.09)  $pk'^c_{(1)1} = 5.89$  and  $pk'c_{(2)1} = 9.49$  at  $\mu = 0.75$  (see Fig. 2 and curve segment in Fig. 4);  $pk'^m_{(1)1} = 5.89 - 0.005$  and  $pk'^m_{(2)1} = 9.49 - 0.005$ . The correction for the change of concentration scale is somewhat smaller than in pure NaCl solutions and is based on a total salt content of 36.4g and the corresponding density of sea water 1.025 at 22°C (13).

Effect of Ca and Mg and the apparent ionization functions  $k''_{(1)}$  and  $k''_{(2)}$ .—The shape of the curves of



Fig. 6. Glass electrode emf shifts produced by the addition of MgSO<sub>4</sub>, MgCl<sub>2</sub>, CaCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub> to bicarbonate and carbonate buffers at atmospheric pressure. A. [HCO<sub>3</sub>] + [CO<sub>3</sub><sup>=</sup>] 0.05 - 0.09 in 0.5 NaCl: Curve 1, effect of Na<sub>2</sub>SO<sub>4</sub> (0.030); Curve 2, effect of MgSO<sub>4</sub> (0.030), MgCl<sub>2</sub> (0.026), and CaCl<sub>2</sub> (0.010). Precipitates are obtained at points 2, 3, and 4; result at pmH 4.8 corresponds to [HCO<sub>3</sub><sup>=</sup>] + [CO<sub>3</sub><sup>=</sup>] 0.022; Curve 3, effect of MgSO<sub>4</sub> (0.030) and MgCl<sub>2</sub> (0.026); Curve 4, effect of MgCO<sub>4</sub> (0.056). B. [HCO<sub>3</sub><sup>-</sup>] + [CO<sub>3</sub><sup>=</sup>] = 0.0025. (2'), (3'), (4') same as (2), (3), (4).

Fig. 6 which give the emf shifts resulting from the addition of Ca and Mg salts to bicarbonate and carbonate buffers can be understood if one bears in mind that removing a constant amount of  $CO_3$ <sup>=</sup> produces a pmH shift which is maximum at  $pmH = \frac{1}{2}(pk'^m_{(1)})$ +  $pk'^{m}(2)$ ). When the trapped CO<sub>3</sub><sup>=</sup> is a function of the initial CO<sub>3</sub><sup>=</sup> concentration, the maximum is broadened and shifted toward a more alkaline pmH. Removing  $HCO_3^-$  produces no shift at  $pm\dot{H} = \frac{1}{2}(pk'^m_{(1)} + pk'^m_{(2)})$ , but results in an acidification or an alkalinization at more acid or more alkaline pmH values; HCO<sub>3</sub><sup>-</sup> trapping is evident in Fig. 6 in the acid range especially when CaCl<sub>2</sub> is added to the more concentrated buffers already containing MgSO4 and MgCl<sub>2</sub>, but the same operation produces a precipitate at pmH > 8.1. No precipitates are observed in the diluted buffers. The data gathered in Fig. 6 can be used to calculate the dissociation constants of MgCO<sub>3</sub>, CaCO<sub>3</sub>, MgHCO<sub>3</sub><sup>+</sup>, and CaHCO<sub>3</sub><sup>+</sup> as Garrels et al. (12) have done from paH determinations on bicarbonate and carbonate buffers before and after addition of CaCl<sub>2</sub> and MgCl<sub>2</sub>. This problem, which involves lengthy calculations, is quite beyond the scope of the present paper and will not be dealt with.

However, at  $pmH_1 \ge 8.0$ , Fig. 6 makes it possible to evaluate the apparent second ionization function of carbonic acid,  $k''_{(2)}$ , in presence of Ca<sup>++</sup>, Mg<sup>++</sup>, and SO<sub>4</sub><sup>=</sup> ions.

For buffers where  $[\text{HCO}_3^{-}] + [\text{CO}_3^{=}] = 0.0025$ , the emf shift due to the addition of 0.030 MgSO<sub>4</sub>, 0.026 MgCl<sub>2</sub>, and 0.010 CaCl<sub>2</sub> is equal to 38.0 mv at  $pmH_1 \simeq 8.3$ . With  $pk'c_{(2)1} = 9.67$  in the pure buffer, this leads to  $pk''c_{(2)1} = 9.67 - 0.65 = 9.02$  at  $\mu = 0.73$ ; at  $\mu = 0.75$ ,  $pk''c_{(2)1} = 9.015$ .

More refined calculations taking into account the true ionization functions  $k^{c}_{(1)}$  (5.89) and  $k^{c}_{(2)}$  (9.49), the equilibrium  $2\text{HCO}_3^- \rightleftharpoons \text{CO}_3^= + \text{H}_2\text{CO}_3$  which is displaced when  $\text{CO}_3^=$  is removed, give a mean value of 9.015  $\pm$  0.015 at  $\mu = 0.75$  in the  $pm\text{H}_1$  interval 7.9-8.5, with a minimum at 8.3 where  $pk^{\prime\prime}c_{(2)1} = 9.00$ . On the molal scale  $pk^{\prime\prime}m_{(2)} = 9.015 - 0.005$ , again at  $\mu = 0.75$ .

The agreement between the directly evaluated value of  $pk''^{c}_{(2)1}$  and the calculated one, implies that, in first approximation,  $HCO_3^{-}$ -trapping by  $Mg^{++}$  and  $Ca^{++}$ must be very small at  $pmH_1 \geq 8.0$ . Trapping of  $HCO_3^{-}$  to a greater extent than Na ions do, would lead to an apparent lowering of  $pk'^{c}_{(1)}$  and also affect  $pk''^{c}_{(2)1}$  but in a more complicated way, depending on pH. This problem will not be discussed here, and it will be assumed that between  $pmH_1$  7.9 and 8.5 it is not necessary to introduce a first apparent ionization function, or that  $pk''^{c}_{(1)} = pk'^{c}_{(1)}$  in buffers where  $[CO_3^{-}] + [HCO_3^{-}] = 0.0025$ .

Since  $pk''^{c}{}_{(2)1} - pk'^{c}{}_{(2)1} = 0.48$ ,  $[CO_3^{=}]_T \simeq 3 [CO_3^{=}]$ and  $[Mg - CaCO_3] \simeq 2 [CO_3^{=}]$ . At  $pmH_1 \ 8.0 [HCO_3^{-}]$ +  $[CO_3^{=}] = 0.0025$ ,  $[CO_3^{=}] = 7.34 \ 10^{-5}$ ,  $[Mg - CaCO_3] = 1.45 \ 10^{-4}$  or 0.22% of the total Ca and Mg concentrations, which is of the order of magnitude (0.28%) given by Garrels *et al.* (12, 15).

In buffers where  $[CO_3^{=}] + [HCO_3^{-}] = 0.09$ ,  $pk''^{c}{}_{(2)1}$  at  $pmH_1$  8.1 is found equal to 9.12 when directly evaluated from curve 2, Fig. 6A, and equal to 9.10 when calculated at  $\mu = 0.84$ , taking reaction  $2HCO_3^{-} \rightleftharpoons CO_3^{=} + H_2CO_3$  into consideration and neglecting the possibility of  $HCO_3^{-}$  trapping in the alkaline range. The apparent ionization function  $pk''^{c}{}_{(2)1}$  is thus not only dependent on pH but also on the concentration of the buffering species. This remark is important and needs be taken into consideration when dealing with data to be valid in natural sea water.

True and apparent ionization functions of carbonic acid, in presence of Mg<sup>++</sup>, Ca<sup>++</sup>, and SO<sub>4</sub><sup>=</sup>, in NaCl solutions at 1000 kg.  $cm^{-2}$  ( $\mu = 0.75$ ).—Comparison of curves 1 and 2 in Fig. 5 shows that  $\Delta E_{1000}$  observed in pure buffer solutions is reduced by a constant amount in the presence of 0.030 Na<sub>2</sub>SO<sub>4</sub>, between  $pmH_1$  6 and 9.5 (the reference 0.01 HCl + 0.49 NaCl solution has again the same salt composition as the buffer under test and  $m_{\rm H^+}$  is assumed to be equal to  $m_{\rm HCl}$ ).

Curve 3 indicates that  $\Delta E_{1000}$  drops progressively from 20.0 mv at  $pmH_1 = 6.0$  to 13.1 mv at  $pmH_1 = 7.90$ in 0.05 NaHCO<sub>3</sub> + 0.5 NaCl solutions containing 0.030 MgSO<sub>4</sub>, 0.026 MgCl<sub>2</sub>, and 0.010 CaCl<sub>2</sub> at various concentrations of CO<sub>2</sub>.

At pH > 8.1 pressure has been applied to the solutions containing the precipitate (see p. 334). The reported emf shifts correspond to the measurements made during the second or third pressure run. The first run generally gives rather unstable values.

Nearly the same emf shifts are observed at  $pmH_1$ 7.8-7.9 with 0.04 MgSO<sub>4</sub> or 0.030 MgSO<sub>4</sub> + 0.026 MgCl<sub>2</sub> with or without 0.010 CaCl<sub>2</sub> (also see Fig. 1 and 3). Lowering of the total CO<sub>2</sub> concentration has not a great effect either. At  $[CO_3^{-}] + [HCO_3^{-}] = 0.0025$ , where no precipitates are observed, the results (indicated by arrows and curve segment 6 in Fig. 5) are about 0.3-0.4 mv lower than those obtained with buffers where  $[CO_3^{-}] + [HCO_3^{-}]$  is between 0.09 and 0.05.

When both NaCl and Mg-Ca salt concentrations are reduced it can be seen from Fig. 1 and 3 that extrapolation to  $\mu = 0$  again gives  $-\Delta V_{1}^{0} = 25.4$  cm<sup>3</sup> mole<sup>-1</sup>. The scattering of the results can be explained by the large *p*H dependence of  $\Delta E_{1000}$  in the alkaline range.

Adding 0.056 MgCl<sub>2</sub> alone to 0.5 NaCl + 0.05 NaHCO<sub>3</sub>, saturated with CO<sub>2</sub>, has no or little effect on  $\Delta E_{1000}$  observed in pure bicarbonate buffer (Fig. 5, curve 4). Between  $pmH_1$  6.2 and 7.85,  $\Delta E_{1000}$  falls from 22.3 mv to 16.0 mv. The 6.3 mv difference is nearly the same as the 6.5 mv value obtained with 0.030 MgSO<sub>4</sub> + 0.026 MgCl<sub>2</sub> for the same  $pmH_1$  interval. The difference between curve 3 and 4 is obviously due to the sulfate ions, since the total Mg concentration is kept constant.

We already have noticed a similar effect of  $SO_4^=$ when 0.030 Na<sub>2</sub>SO<sub>4</sub> is added to pure bicarbonate buffers (curves 1 and 2 in Fig. 5). The fact that MgSO<sub>4</sub> is less dissociated than Na<sub>2</sub>SO<sub>4</sub> probably explains the difference in magnitude between the effects of 0.030 Na<sub>2</sub>SO<sub>4</sub> and 0.030 MgSO<sub>4</sub>. Since the ordinate difference between curve 4 and 3 is nearly constant, the SO<sub>4</sub><sup>=</sup> effect of MgSO<sub>4</sub> practically must be constant over the whole *pm*H<sub>1</sub> range. This observation allows one to extrapolate curve 3 parallel to curves 2 and 1 in the alkaline range (curve 3') and to dissociate the SO<sub>4</sub><sup>=</sup> effect from the more complicated Mg-Ca effect observed between 6.5 and 9.0.

To interpret the Mg-Ca effect, we will assume that the MgCO<sub>3</sub> and CaCO<sub>3</sub> ion pairs, formed at atmospheric pressure, further dissociate at higher pressures, liberating  $CO_3^{=}$  ions which alter the  $[CO_2]/[CO_3^{=}]$ ratio of the buffer, eventually shift reaction 2HCO3- $\Rightarrow$  CO<sub>3</sub><sup>=</sup> + H<sub>2</sub>CO<sub>3</sub>, and thus oppose the acidification induced by pressure and caused by the dissociation constants shifts. This assumption leads to the admission that log  $k'^{m_{1000}}/k'^{m_{1}}$ , in presence of MgCl<sub>2</sub> has the same value, for each true ionization function, as found in pure bicarbonate buffer at the same  $pmH_1$ and ionic strength, not only between  $pmH_1$  5.5 and 7.0, but throughout the whole pmH1 range. When MgSO4 is substituted for part of the MgCl<sub>2</sub>, log  $k'^{m}_{1000}/k'^{m}_{1}$ is lowered by an amount corresponding to the  $SO_4$ = effect. One can then use the same arguments developed above and measure  $pk'_{(1)}$  and  $pk'_{(2)}$  at  $pmH_1$ 7.0 and 8.5, respectively, on curve 3 and 3'.

One thus finds that at  $\mu = 0.75$ ,  $[CO_3^{=}] + [HCO_3^{-}] = 0.0025$ , log  $k'^{m}_{1000}/k'^{m}_{1} = 0.316$  (18.5 mv) for  $k'_{(1)}$  and 0.283 (16.5 mv) for  $k'_{(2)}$ . In more concentrated buffers, these values become 0.325 (19.0 mv) and 0.290 (17.0 mv) at the same ionic strength and  $pmH_1$ .

At  $pmH_1$  8.5, Fig. 5 further allows to obtain a direct estimate of the effect of pressure on the apparent ionization function  $pk''_{(2)}$ . At  $[HCO_3^-] + [CO_3^-] = 0.0025$ , log  $k''^m_{(2)1000}/k''_{(2)1} = 0.178$  ( $\Delta E_{1000} = 10.4$  mv). A more elaborate treatment using  $pk'^{m}_{(1)1000}$ and  $pk'^{m}_{(2)1000}$ , taking into account the equilibrium  $2\text{HCO}_3^- \rightleftharpoons \text{CO}_3^= + \text{H}_2\text{CO}_3$ , the amount of MgCO<sub>3</sub> formed at atmospheric pressure, shows that log  $k''^{m}_{(2)1000}/k''^{m}_{(2)1}$  increases from 0.178 at  $pm\text{H}_1$  8.5, to 0.187 at 8.0, 0.190 at 7.9, and 0.214 at 7.6. A mean value of 0.183  $\pm$  0.005 can be taken in the  $pm\text{H}_1$  interval 8.0-8.5. The same value can be read from Fig. 5 at  $pm\text{H}_1 = 8.5$  for the more concentrated buffers.

The effect of pressure on  $pk''_{(1)}$  needs not be considered in the alkaline range since we have admitted that between  $pmH_1$  7.9 and 8.5,  $pk'_{(1)} = pk''_{(1)}$ . At  $pmH_1 \leq 7.0$ , comparison of the curves of Fig. 5 and 6 for the more concentrated buffers, where HCO<sub>3</sub><sup>-</sup> trapping by Ca<sup>++</sup> seems obvious, shows that pressure must have only a very small effect on the dissociation of any trapped HCO<sub>3</sub><sup>-</sup> ions.

Dissociation of carbonic acid in natural sea water  $(Cl = 20\%_0)$  at high pressures; effect of boric acid.— The reference compartment of the glass electrode contains 0.49 NaCl, 0.01 HCl, 0.030 MgSO<sub>4</sub>, 0.026 MgCl<sub>2</sub> and 0.010 CaCl<sub>2</sub>.

The sea water samples come from the Atlantic Ocean (north of Spain, Cl  $\%_0 = 19.5$ ) and have been equilibrated with  $CO_2 + N_2$  mixtures, or small amounts of  $Na_2CO_3$  have been added to cover the 5.0-9.0  $pmH_1$ interval. The emf shifts produced by increasing pressure from 1 atm to 1000 kg. cm<sup>-2</sup> are corrected in Fig. 5 at  $\mu = 0.75$  (Cl %<sub>0</sub> = 20.0). Scattering is higher than with artificial buffers; nevertheless, it is obvious that from  $pmH_1$  5.0 to about 7.25 (curve 5), sea water follows the general pattern observed in bicarbonate buffers with added Mg, Ca, and sulfate ions. The quantitative agreement is good, although the data for natural sea water are about 0.3-0.4 my below these for artificial sea water (arrows in Fig. 5). Extrapolation of the curve drawn in the acid range (curves 5 and 5'), parallel to curves 1, 2, 3', allows one to obtain log  $k'^{m_{1000}}/k'^{m_{1}}$  for the first and second dissociation step: 0.314 (18.3 mv) and 0.278 (16.3 mv), respectively, at  $pmH_1 = 7.0$  and 8.5. This corresponds to the shift of the true ionization functions which are assumed to have the same value at 1 atm as the corresponding functions determined in artificial sea water (see above).

At pH > 7.25, the data for natural sea water progressively depart from the results in artificial sea water containing Mg<sup>++</sup>, Ca<sup>++</sup>, and SO<sub>4</sub><sup>=</sup>. At pH 8.5-9.0,  $\Delta E_{1000}$  is about 3.0 mv higher in natural sea water and to nearly duplicate these results, 0.43 10<sup>-3</sup> H<sub>3</sub>BO<sub>3</sub> must be added, the  $pmH_1$  being adjusted by the  $[HCO_3^-]/[CO_3^=]$  ratio (curve 6', Fig. 5). The ordinate difference between curve 6' and the corresponding emf shifts observed in artificial sea water without boric acid is given by curve 7 which shows the effect of boric acid between  $pmH_1$  6.5 and 9.0.

Preliminary experiments to investigate the effect of pressure on the dissociation of boric acid show that in NaCl 0.1,  $\Delta V_1$  extrapolates to  $-29.0 \text{ cm}^3 \text{ mole}^{-1}$ at zero borate buffer  $(H_3BO_3 + borax)$  concentration, to -30.7 cm<sup>3</sup> mole<sup>-1</sup> in NaCl 0.01 and to -31.4 cm<sup>3</sup> mole<sup>-1</sup> in NaCl 0.001;  $\Delta V_1^{\circ} = -32.1 \text{ cm}^3 \text{ mole}^{-1}$ . In  $0.5 \text{ NaCl} + 0.030 \text{ MgSO}_4 + 0.026 \text{ MgCl}_2 \text{ and } 0.010 \text{ CaCl}_2,$ at pH 7.9,  $\Delta V_1$  is equal to  $-23.1 \text{ cm}^3 \text{ mole}^{-1}$  (22.7 mv) at zero borate concentration, and the same value can be used at the boron concentration of sea water. Since in sea water  $pk'^{m}_{(1)1} = 8.605$  for boric acid  $(pk'^{c}_{(1)1} -$  $\log y_{H^+} = pK''^c{}_{(1)1} = 8.72$  [Lyman (13],  $pk'^m{}_{(1)1000} = 8.605-0.39 = 8.215$ . These values correspond fairly well to the  $pmH_1$  at which curve 7 of Fig. 5 reaches a maximum. It is also easy to verify that at  $pmH_1 =$ 8.353 and  $[HCO_3^-] + [CO_3^-] = 0.0025$ , the increase in  $HCO_3^-$  concentration at 1000 kg. cm<sup>-2</sup> (pmH<sub>1000</sub> = 8.124), calculated from the values of  $pk''^{m}(2)$  and  $pk'^{m}(1)$  for carbonic acid, obtained in artificial sea water without boric acid, corresponds to the decrease in H<sub>3</sub>BO<sub>3</sub> concentration, estimated from  $pk'^{m}_{(1)1}$  and

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 $pk'^{m}_{(1)1000}$  found for boric acid in sea water  $(\Delta[\text{HCO}_3^{-}]_T = 0.39 \ 10^{-4}; \ \Delta[\text{H}_3\text{BO}_3] = 0.38 \ 10^{-4}).$ 

The interpretation of the pH changes induced by pressure in natural sea water is thus far from simple. The enhanced dissociation of carbonic acid observed in NaCl at the corresponding ionic strength is modified by the presence of sulfate ions, by the dissociation of MgCO<sub>3</sub> and CaCO<sub>3</sub>, and by the dissociation of boric acid. The two last effects are pH dependent, and reaction H<sub>3</sub>BO<sub>3</sub> + CO<sub>3</sub><sup>=</sup>  $\Rightarrow$  HCO<sub>3</sub><sup>-</sup> +H<sub>2</sub>BO<sub>3</sub><sup>-</sup> must be considered.

Without going into the details of a quantitative analysis, it is immediately clear that the emf shifts observed at  $pmH_1 > 8.0$  in artificial sea water containing boric acid or in natural sea water cannot be used for a direct estimation of  $\Delta p k''_{(2)} / \Delta p$  for the second apparent ionization function; instead,  $pk''_{(2)p}$  has to be taken equal to the corresponding function determined in artificial sea water without boric acid in order to calculate  $[CO_3^{=}]_T$  and  $[HCO_3^{-}]_T$  at pressure p. In artificial sea water, in absence of boric acid, log  $k''^m_{(2)1000}/k''^m_{(2)1} = 0.183 \pm 0.005$  from  $pmH_1$  8.0 to 8.5; in natural sea water, since  $\Delta E_{1000}$  is somewhat lower, log  $k''^{m}_{(2)1000}/k''^{m}_{(2)1}$  will be taken equal to  $0.178 \pm 0.005$  in the same  $pmH_1$  interval. If the greatest precision is required, the pH dependence of log  $k''^m_{(2)1000}/k''^m_{(2)1}$  must be taken into account (see p. 335). The value of  $pk''^{m}(2)$  at 1 atm found in artificial sea water without boric acid (9.01, see p. 334) is taken to be the same in natural sea water. The complete set of ionization functions which we believe to be valid in natural sea water at 1 atm and at 1000 bars, within our basic assumptions, is given in Table II.

Some of the results of Fig. 5 have been indicated in Fig. 1 together with data obtained with 0.01 HCl + 0.49 NaCl as reference half-cell, and which are in agreement with our earlier results (4).  $\Delta E_{1000} = 16.7$ mv instead of 13.4 mv at  $pmH_1$  7.8; the difference of 3.3 mv is due to the effect of pressure on  $\gamma_{HCl}$  in the presence of MgSO<sub>4</sub> + MgCl<sub>2</sub> + CaCl<sub>2</sub> compared to  $\gamma_{HCl}$  in pure HCl or HCl + NaCl (see below). Dilution of sea water leads to erratic pressure-induced emf shifts, but sea water + 0.05 NaHCO<sub>3</sub>, CO<sub>2</sub> 1% can be diluted, and the extrapolation of the results to  $\mu = 0$  gives  $\Delta V_1^{\circ} = -25.4$  cm<sup>3</sup> mole<sup>-1</sup> identical with the value found in pure bicarbonate (Fig. 1).

Apparent values of  $\gamma_{\rm HCl}$ ,  $y_{\rm H^+}$  in HCl + NaCl in presence of Mg<sup>++</sup>, Ca<sup>++</sup>, SO<sub>4</sub><sup>=</sup>; effect of pressure.— The apparent mean activity coefficient of 0.01 HCl on the molal scale in presence of 0.5/n - 0.01 NaCl, MgSO<sub>4</sub>, MgSO<sub>4</sub> + MgCl<sub>2</sub>, MgSO<sub>4</sub> + MgCl<sub>2</sub> + CaCl<sub>2</sub> is given in Fig. 7 for several values of *n* assuming  $m_{\rm H^+} = m_{\rm HCl}$ . The reference half-cell was filled with HCl 0.01, NaCl 0.09. The data for pure NaCl or KCl + HCl solutions are taken from Harned and Owen (10), and control experiments show that our results fit these curves with an error not greater than  $\pm$  0.002. From Eq. [6], log y can be calculated from log  $\gamma$ : in NaCl solutions at  $\mu = 0.5 \log \gamma = \log y -$ 0.004; the correction factor is -0.0047, -0.0055, -0.063,-0.0071, -0.008 at  $\mu = 0.6, 0.7, 0.8, 0.9, 1.0,$  and -0.006at  $\mu = 0.75$ . At  $\mu = 0.75$  in sea water, the correction becomes -0.004.

MgCl<sub>2</sub> alone has a much smaller effect on  $\gamma_{\rm HCl}$ : addition of 0.056 MgCl<sub>2</sub> to 0.49 NaCl + 0.01 HCl makes log  $\gamma_{\rm HCl}$  drop from  $\overline{1.864}$  to  $\overline{1.849}$ .

The pressure dependency of  $\gamma_{HC1}$  in 0.01 HCl + 0.49 NaCl containing MgSO<sub>4</sub>, MgSO<sub>4</sub> + MgCl<sub>2</sub> is represented in Fig. 8 either with 0.01 HCl + 0.49 NaCl as reference half-cell or 0.1 HCl. It is clear that MgSO<sub>4</sub> is the main cause involved.

In the preceding sections, it has been assumed continuously that  $\gamma_{HCI}$  measured in 0.01 HCl + 0.49 NaCl + 0.030 MgSO<sub>4</sub> + 0.026 MgCl<sub>2</sub> + 0.010 CaCl<sub>2</sub> has the same value in carbonate and bicarbonate buffers containing the same salts, in the range [CO<sub>3</sub>=] + [HCO<sub>3</sub><sup>-</sup>] = 0.09 - 0.0025. That the specific salt effect



Fig. 7. Mean activity coefficient ( $\gamma_{HCl}$ ) of HCl in NaCl, KCl; apparent values in presence of MgSO<sub>4</sub>, MgCl<sub>2</sub>, CaCl<sub>2</sub> as a function of  $\sqrt{\mu}$ .

of CO<sub>2</sub>, CO<sub>3</sub><sup>=</sup>, HCO<sub>3</sub><sup>-</sup> is small, is demonstrated by Fig. 1, 2, 3, and 4, where it can be seen that changing the buffer concentration (at a given buffer ratio for Fig. 2 and 4) has about the same effect as changing the ionic strength. Comparison of the data of Fig. 5 further shows that lowering the  $[CO_3^{=}] + [HCO_3^{-}]$ concentration from 0.09 to 0.0025 has only a very small effect on  $\Delta E_{1000}$  at a given ionic strength (0.75).

Figure 7 also indicates that  $\gamma_{\text{HCl}}$  is fairly independent of  $\mu$  in the region of the ionic strength of sea water. Corrections for salinity differences are thus very small; corrections however have to be made to take into account the eventual difference in Cl<sup>-</sup> content between both glass electrode compartments, in order to calculate —log [H<sup>+</sup>], assuming  $\gamma_{\text{HCl}}$  to be equal in both solutions. Ordinary *pa*H electrodes with liquid junctions at first sight appear to be simpler to use, since the exact composition of the reference glass electrode halfcell does not have to be known with precision. However, conventional *pa*H electrodes display a much more sluggish response and great errors can be introduced



Fig. 8. Effect of pressure on 2 log  $(\gamma_{\rm HCl})^{\rm ref}_1/(\gamma_{\rm HCl})^{\rm ref}_p - 2$  log  $(\gamma_{\rm HCl})^x_1/(\gamma_{\rm HCl})^x_p$  2.3 RT/F =  $E_1 - E_p$ , where ref and x correspond to the inner and outer compartment of the glass electrode cell; effect of MgSO<sub>4</sub> and MgCl<sub>2</sub>.

However, since most of the oceanographic data refer to paH measurements, we have tried to measure paH at atmospheric pressure in mixtures of HCl + NaCl or  $KCl + MgSO_4 + MgCl_2 + CaCl_2$ . Saturated KCl agaragar junctions were used with calomel electrodes as inner and outer electrodes of the glass cell. Stable and reproducible results have been obtained in KCl with 0.01 HCl + 0.09 KCl in the reference compartment. The value indicated on Fig. 9 for log  $a_{H+}$  in 0.01 HCl + 0.09 KCl was checked with a hydrogen electrode-calomel electrode cell, and is close to the value reported in Harned and Owen (10), 3.898. The hydrogen ion activity in HCl + KCl was first measured, and the effect of the added salts was investigated either with 0.01 HCl + 0.09 KCl as inner solution or with 0.01 HCl + 0.5/n - 0.01 KCl, n being equal on both sides of the glass electrode. Trying to measure  $a_{\rm H+}$  in HCl + NaCl with 0.1 HCl as inner solution resulted in erratic information. Reproducible data could only be obtained by systematically using KCl + HCl at the same ionic strength as inner solution.

The curves giving  $\log a_{\rm H+}$  in HCl + NaCl in presence of Mg and Ca salts have been determined by taking 0.5/n NaCl - 0.01 HCl for inner solutions and



Fig. 9. Hydrogen ion activity (log  $a_{\rm H}$ +), in 0.01 HCI + NaCl or KCl, in presence or not of MgSO<sub>4</sub>, MgCl<sub>2</sub>, CaCl<sub>2</sub> as a function of  $\sqrt{\mu}$  (glass electrode with calomel electrodes and sat. KCl agar-agar salt bridges).

making *n* equal in both compartments. If one takes  $c_{\rm H+} = c_{\rm HCI}$ , log  $y_{\rm H+}$  at  $\mu = 0.75$  is 1.887 and one then can assume that it nearly has the same value in sea water. Anderson and Robinson (14) estimate log  $y_{\rm H+}$  equal to 1.880 in sea water (Cl = 20.0%<sub>o</sub>) acidified to pH 3.3-3.9 with HCl, which is not too far from our value for log  $y_{\rm H+}$ .

Evaluation of apparent dissociation constants  $y_{\rm H}+k'^{c}{}_{(1)} = K''^{c}{}_{(1)}$  and  $y_{\rm H}+k''^{c}{}_{(2)} = K''^{c}{}_{(2)}$  of carbonic acid in sea water at 1 atm and 1000 kg. cm<sup>-2</sup>,—The apparent constants used in oceanography are defined as  $K''^{c}{}_{(1)} = a_{\rm H} + \times [{\rm HCO}_3^{-}]_T/[{\rm CO}_2] = y_{\rm H} + k'^{c}{}_{(1)}$  and  $K''^{c}{}_{(2)} = a_{\rm H} + \times [{\rm CO}_3^{-}]_T/[{\rm HCO}_3^{-}]_T = y_{\rm H} + k'^{c}{}_{(2)}$ , where T refers to total concentrations. Since  $\gamma m = yc/do$  (Eq. [7]) it follows that  $pK''^{m}{}_{(1)(2)} = pK''^{c}{}_{(1)(2)}$ —0.001 at 1 atm.

According to Lyman (13),  $pK''^{c}{}_{(1)} = 6.00$  and  $pK''^{c}{}_{(2)} = 9.12$  at 22°C, Cl %<sub>0</sub> = 20.0. Taking our values  $pk''^{c}{}_{(1)1} = 5.89$ ,  $pk''^{c}{}_{(2)1} = 9.015$  valid for artificial sea water in the  $pmH_1$  interval 7.9-8.5, and  $-\log$  $y_{\rm H^+} = 0.11$ , gives  $pK''c_{(1)} = 6.00$  and  $pK''c_{(2)} = 9.125$ which is in good agreement. Since  $pk'^{c}(1)$  has been determined at pmH1 5.0 where obviously HCO3<sup>-</sup> trapping by Mg and Ca is very small or inexistent (see Fig. 6A), but where the effect of  $SO_4^=$  can be measured, and since  $pk'^{c}{}_{(1)}$  fits with the  $pK''^{c}{}_{(1)}$  value given by Lyman, one comes to the conclusion that at alkaline pH,  $HCO_3^-$  trapping by Mg and Ca must be small in sea water, or that the  $HCO_3^-$  bound to Mg or Ca cannot be distinguished from that linked to Na. The problem is however not completely solved since in more concentrated buffers  $([CO_3^{=}] + [HCO_3^{-}] =$ 0.05 - 0.09) HCO<sub>3</sub><sup>-</sup> binding by Ca and Mg is obvious at  $pmH_1$  7.0. Further analysis of these results and more experiments will be needed to decide whether or not  $HCO_3^-$  trapping persists in the alkaline range when  $CO_3$ <sup>=</sup> binding reaches its maximum, and to find out how it depends on the buffer concentration.

To estimate the effect of pressure on  $pK''_1$  and  $pK''_2$ , the pressure dependence of  $\gamma_{\rm H+}$  needs be known. It cannot be calculated in media as complex as sea water. Since however this uncertainty affects both pK'' and paH identically, it has no bearing on the determination of the ratios  $[CO_3^=]_T/[HCO_3^-]_T$ ,  $[CO_3^=]_T/[CO_2]$  and  $[HCO_3^-]_T/[CO_2]$  needed in oceanographic calculations to compute  $[CO_2]$ ,  $[HCO_3^-]_T$   $[CO_3^=]_T$  from paH,  $pK''_{(1)}$ ,  $pK''_{(2)}$ , and  $\Sigma CO_2 = [CO_2] + [HCO_3^-]_T +$  $[CO_3^=]_T$ . The simplest assumption, which is to neglect the effect of pressure on  $\gamma_{\rm H+}$ , leads to admit that  $\Delta pK''m_{(1)(2)}/\Delta p = \Delta pk''m_{(1)(2)}/\Delta p$ , so that in natural sea water at 1000 kg. cm<sup>-2</sup>,  $pK''m_{(1)}$  and  $pK''m_{(2)}$  would respectively, be equal to 6.00 - 0.314 and 9.125 - 0.178(see p. 336) whereas  $pK''c_{(1)}$  and 9.125 - (0.178 + 0.017), between  $pmH_1$  8.0 and 8.5.

According to Buch and Gripenberg (16), the change of  $pK''^{m}{}_{(1)}$  and  $pK''^{m}{}_{(2)}$  with pressure are, respectively, 0.480 and 0.180 at 1000 bars, or 0.470 and 0.176 at 1000 kg. cm<sup>-2</sup>. Their values were based on  $\Delta V_{1^0} = -28.0$ cm<sup>3</sup> mole<sup>-1</sup> for the first ionization step of carbonic acid and  $\Delta V_{1^0} = -10.5$  cm<sup>3</sup> mole<sup>-1</sup> for the second step assuming that the HCO<sub>3</sub><sup>-</sup> ion would behave as acetic acid. Curiously enough our data fit almost exactly for  $K''_{(2)}$ , although the reasons of the small effect of pressure on  $K''_{(2)}$  are completely different from what these authors thought them to be. As we already indicated,  $pk''_{(2)}$  and  $pK''_{(2)}$  either on

As we already indicated,  $pk''_{(2)}$  and  $pK''_{(2)}$  either on the molar or molal scale, determined in artificial sea water without boric acid at pressure p will give correct estimates for  $[HCO_3^-]_T$  and  $[CO_3^-]_T$  in the  $pmH_1$ range 8.0-8.5, and it is theoretically possible, taking the boric acid effect into consideration, to calculate the pmH, pcH, or paH of a given surface sea water sample brought to pressure p, or at the corresponding depth. It is however much more easy to read  $\Delta pmH/\Delta p$ from Fig. 5, or to use Table I where we have given the paH shifts on the molar scale in natural sea water

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Table I. paH at 1 atm and 1000 bar in natural sea water, molar scale\*, CI %<sub>o</sub> 20.0

paH at 1 atm	7.5	7.6	7.7	7.8	7.9	8.0
paH at 1000 bars		1.97				Te la la
Buch and Gripen-		7 90	7 49		7 07	7 70
This paper (10)	7.10	7.29	7.40	7.50	7.69	7.74
this paper (a)	7.20	7 21	7.41	7 525	7.65	1.14
	1.20	1.01	1.12	1.000	1.00	
paH at 1 atm	8.1	8.2	8.3	8.4	8.5	8.6
paH at 1000 bars Buch and Gripen-			1	5-10		1
berg (16)	7.89	8.00	8.10	8.20	8.30	-
This paper	7.85	7.95	8.05	8.155	8.255	8.355

• log  $y_{\rm H}$ <sup>+</sup> $c_{\rm H}$ <sup>+</sup> = log  $\gamma_{\rm H}$ <sup>+</sup> $m_{\rm H}$ <sup>+</sup> + 0.016 at 1000 bars (c, molar scale, m, molal scale); log  $\gamma_{\rm H}$ <sup>+</sup> is assumed not to vary with pressure;  $\sim \log \gamma_{\rm H_1}$ <sup>+</sup> = 0.114 and  $-\log y_{\rm H_1}$ <sup>+</sup> = 0.11.

predicted on the basis of Buch and Gripenberg's (16) estimates of pK"(2) and pK"(1) at 1000 bars and our experimental rounded off data.

The two series of values from paH 7.5 to 8.0 reflect the scattering of the results of Fig. 5; to obtain set (a), 0.3 my where substracted from curve 6' to take into account the difference between the results in artificial and natural sea water; set (b) corresponds to curve 3 between 7.5 and 7.9. To adapt these values to other types of water small corrections will have to be made to take into account differences in salinity,  $SO_4^{=}$ , Mg, Ca, and boric acid content.

The set of ionization functions and apparent dissociation constants based on the experiments described in this paper is given in Table II.

It is important to keep in mind that the ionization functions k', k'', and also K'' in Table II, can only be used to interpret emf measurements made with one particular type of reference half-cell. If other cells are used corrections have to be made affecting pmH and pk' identically.

#### Conclusions

A coherent set of ionization functions has been established on the molal and the molar concentration scales, from 1 atm to 1000 kg. cm<sup>-2</sup> and at 22°C for carbonic acid in NaCl (KCl) over a wide range of ionic strengths, in the presence of Mg++, Ca++, and  $SO_4$  = ions, and in sea water. It allows the use of pmH or pcH measurements with a junctionless glass electrode cell and  $\Sigma CO_2$  determinations to calculate the concentrations of  $CO_2$ ,  $HCO_3^-$ ,  $CO_3^=$  (free and bound to Na, Mg, and Ca). Data are also available to take into account the increased dissociation of boric acid in natural sea water at high pressure. Corrections are given for different types of reference half-cells.

In situ paH, pcH, or pmH values at any ocean depth have been determined for one type of surface water (Atlantic Cl = 20.0%) and can simply be read from the experimental curve giving  $\Delta pmH/\Delta p$  as a function of pmH, at 1 atm and 22°C, in the pmH interval 5.0-9.0. The data can be used at any other temperature if one assumes that the temperature coefficient of the ionization functions is independent of pressure or the pressure coefficient is independent of temperature. This assumption however plausible, remains to be proven experimentally. Small corrections for differences in salinity, sulfate, B, Mg, Ca concentrations will have to be established for other water types.

Detailed calculations will be given in a following paper and will be used for the quantitative interpretation of direct in situ pcH or pmH measurement at great ocean depths (5, 6).

The apparent mean activity coefficient of HCl has been measured in NaCl solutions in the presence of  $Mg^{++}$ ,  $Ca^{++}$ , and  $SO_4^{=}$  at atmospheric pressure and at 1000 kg. cm<sup>-2</sup>, and also  $y_{\rm H}$ + at 1 atm. It is thus theoretically possible to calculate  $y_{HCO3}$  - and  $y_{CO3}$  = in the various bicarbonate and carbonate buffers investigated including sea water, since  $y_{CO_2}$  is known with rather good precision (9, 15)

The determination of  $y_{\rm H^+}$  in NaCl in the presence of  $Mg^{++}$ ,  $Ca^{++}$ ,  $SO_4^{=}$  allows correlation of the ionization functions obtained with junctionless glass electrode cells with the so-called apparent dissociation constants widely used in oceanography to calculate  $[CO_3^{=}]_{total}$  and  $[HCO_3^{-}]_{total}$ . The results show that the apparent second dissociation constant is pH dependant with a rather broad minimum between  $pmH_1$ 7.9 and 8.5, where the mean value of  $pK''_{(2)}$  is 9.125 at 1 atm and 22°C. Since  $pK''_{(1)} = 6.00$  at this temperature and pressure, both these values are in agreement with the data of Lyman (13).

Table II. Ionization functions and apparent dissociation constants for carbonic acid in sea water (Cl 20.0 %o) at 22° C valid between paH 8.1 and 8.6a

	1 atm				1000 bar			
Ionization functions	pk'(1)		pk'(2)		pk'(1)		pk'(2)	
$pk' = -\log \frac{[\mathbf{R}^+][\mathbf{R}^-]}{[\mathbf{R}^+]}$	c	m	c	m	c	m	c	m
IUK	5.89 5.89	5.885 5.885	9.49 9.49	9.485 9.485	5.553 5.55	5.565 5.565	9.19 9.19	9.202 9.20
Apparent ionization functions <sup>b</sup>	pk"(1) =	= pk'(1)	р	k" (2)	pk" (1)	$= pk'(\mathbf{u})$	pk'	" (2)
$pk'' = -\log \frac{\Pi \Pi \Pi}{[\Pi R]_T}$	5.89 5.89	5.885 5.885	9.015 9.015	9.01 9.01	5.553 5.55	5.565 5.565	8.817 8.82	8.829 8.83
Apparent oceanogr. dissociation constants	pK	"(1)	р	K″ (2)	pI	<b>X″</b> (1)	pk	۲″ (2)
$pK'' = -\log \frac{a_{\rm H^+} \times [{\rm R}^{-}]_T}{[{\rm HR}]_T}$ (pK'''m <sub>1</sub> = pK'''c <sub>1</sub> - 0.001)	6.00 6.00	$(- \begin{array}{c} 6.00 \\ (- 0.001) \\ 6.00 \end{array})$	9.125 9.125	9.125 (-0.001) 9.125	5.663 5.66	5.68 (-0.001) 5.68	8.927 8.93	8.944 (-0.001) 8.94
	pk'(1), pk	"(1), pK"(1)			pl	c' (2)	pk" (2),	pK" (2)
Tonination functions and dissociation con	c	m			c	m	c	m
stants shift at 1000 bars	0.320 + 0.017°				0.283 + 0.017		0.181 + 0.017	
	0.337	0.320			0.300	0.283	0.198	0.181

<sup>a</sup> log  $\gamma_{H^+}$  is assumed not to vary with pressure; the second row of data corresponds to rounded off values; c and m indicate the molar and molal concentration scale respectively. <sup>b</sup> T indicates total concentrations. <sup>e</sup> 0.017 = log  $d_{1000}/d_1$ , where d is the density.

If one admits that the pressure dependence of  $\gamma_{\rm H}$ + can be neglected, then the effect of pressure, compared with data from Buch and Gripenberg (16), shows fortuitous agreement for the second apparent dissociation constant in the  $pmH_1$  interval 8.0-8.5 (on the molal scale at 1000 bars,  $pK''_{(2)} = 0.181$  against 0.180), but the effect of pressure on the first constant is much less than that predicted by these authors (at 1000 bars,  $pK''_{(1)} = 0.320$  instead of 0.480).

The comparison must be considered with caution since we do not know the absolute values of the ionization functions and apparent dissociation constants, but it shows that one cannot simply assume, as Buch and Gripenberg did, that H2CO3 dissociates at high pressure in sea water in the same manner as at zero ionic strength and that HCO<sub>3</sub><sup>-</sup> behaves as acetic acid.

The reduced effect of pressure on the apparent second dissociation constant of carbonic acid in sea water at  $pmH_1 > 8.0$  corresponds to an apparent volume change of -10.6 cm<sup>3</sup> mole<sup>-1</sup> instead of -25.6 cm<sup>3</sup> mole<sup>-1</sup> observed at 0 ionic strength. This can be understood by taking into consideration : 1° the effect of NaCl on the pressure dependence of the mean activity coefficient of  $H_2CO_3$  and  $HCO_3^-$ ; 2° the effect of sulfate ions which does not depend on pH; and 3° the formation of MgCO3 and CaCO3 at atm pressure which dissociate under pressure, liberating  $CO_3^{=}$  ions which alter the buffer ratio, the whole process being pH dependent.

The increased dissociation of boric acid, the result of which is again a function of the hydrogen ion concentration, explains why the pmH or pcH shift observed in sea water is progressively larger from pmH1 7.0 to 9.0 than that predicted from the effect of pressure on the apparent ionization function of HCO3-, measured in artificial sea water without boric acid. Factors 1°, 2°, and 3°, on the contrary, really or apparently depress the effect of pressure on the ionization of carbonic acid. MgCO3 and CaCO3 thus appear to have a buffering action against hydrogen ion concentration changes induced by pressure in sea water although boric acid progressively and partially counteracts this effect at  $pmH_1$  values greater than 7.0.

Starting from these considerations one might imagine that other buffer systems involving ion pairs or complex ions able to liberate anions capable of binding H<sup>+</sup> ions, could be prepared, where  $\Delta pmH/\Delta p$  would be very small. Such media would be very useful in, for instance, the study of the specific effect of pressure on biological systems. Furthermore, if the effect of pressure on a given acid-base equilibrium is well known, changes produced by the pressure induced dissociation of added ion pairs offer a way to demonstrate their existence at atmospheric pressure.

The results which we have obtained at 1000 kg.  $\rm cm^{-2}$  in pure carbonate and bicarbonate buffers in NaCl or KCl show, for example, that probably more ion pairs exist in NaCl than in KCl, in correlation with the difference observed for the corresponding ionization functions at atmospheric pressure. This observation might prove a clue to interpret the anomalies encountered when  $\Delta V_1^{\circ}$  is computed from glass electrode measurements by extrapolation at zero ionic strength (3). The values obtained in pure acid are always somewhat higher than in the corresponding buffers  $(-26.5 \text{ cm}^3 \text{ mole}^{-1} \text{ in } \text{H}_2\text{CO}_3, -25.4 \text{ cm}^3 \text{ mole}^{-1} \text{ in bicarbonate buffer, for example}).$  This effect could be explained if ion pairs still exist at the highest dilutions which are practical for precise emf determinations.

#### ADDENDUM<sup>1</sup>

Interpretation of the  $SO_4$ =-effect.—It has been assumed in the preceding pages that  $m_{\rm H^+} = m_{\rm HCI} = 0.01$ in the reference half-cells containing 0.03 MgSO<sub>4</sub> and the effect of  $SO_4^{=}$  ions on the observed emf values have therefore been interpreted as a change which affects  $k'_{(1)}$ ,  $k'_{(2)}$ ,  $\gamma_{\rm HC1}$  and  $\gamma_{\rm H+}$ . This "SO<sub>4</sub><sup>=</sup> — effect",

<sup>1</sup> Added on proof.

observed in presence of NaCl + MgCl<sub>2</sub> and CaCl<sub>2</sub>, is uncommonly large and of the same order of magnitude in each case as shown by the data obtained at  $\mu =$ 0.75:

	in NaCl	in sol. + MgSO4	Δ
pk'c(1) pk'c(2)	6.00 9.60	5.89 9.49	0.11 0.11
2 log γHC1	1.734	1.617	0.117
log γ <sub>H</sub> +	0.017	1.887	0.13

Further, at 1000 kg cm<sup>-2</sup>, SO<sub>4</sub><sup>=</sup> ions apparently increase  $pk'_{(1)}$  and  $pk'_{(2)}$  by a constant amount which corresponds to an emf shift between 2.0 and 2.7 mv, depending on the buffer concentration (Fig. 5), where-as the effect of the same pressure on the reference half-cell containing  $SO_4^{=}$  is equal to 3.3 mv (Fig. 8). It actually appears that the greatest part of the  $SO_4^{=}$ – effect must find its explanation in the formation of  $SO_4H^{-}$  ions in the reference half-cell, which invali-dates the accumption mean factor the second dates the assumption  $m_{\rm H^+} = m_{\rm HCl}$  [see Jones and Monk (17)]. Taking  $K_{\rm HS04^-} = 1.13~10^{-2}$ ,  $\gamma_{\rm S04^+} =$ 0.12  $\gamma_{\rm HSO4}$  = 0.68, assuming 54% of the sulfate to be free ions [see the data of Garrels and Thompson for sea water (15)] and  $a_{\rm H^+} = 7.7 \ 10^{-3}$  (paH = 2,113, see Fig. 9), one finds  $pmH_1 = 2.088$  instead of 2.00, which accounts for 80% of the apparent SO<sub>4</sub>= - effect on  $pk'_{(1)}$  and  $pk'_{(2)}$  at 1 atm. One will notice that 2 log  $\gamma_{HCl} = \overline{1.698}$  in 0.01 HCl + 0.49 NaCl + 0.056 MgCl<sub>2</sub> (see p. 336) and that at the same ionic strength, 2 log  $\gamma_{\rm HCl}$  in 0.01 HCl + NaCl is equal to 1.730. Although the salt effects of individual ions are not necessarily additive, the difference 0.032 indicates that the  $SO_4^{=}$  — effect is probably not larger than the cal-culated value 0.088, since the total effect of  $SO_4^{=}$  and  $Mg^{++}$  is equal to 0.117. In other words,  $pmH_1$  in the culated value 0.088, since the total effect of  $SO_4^=$  and  $Mg^{++}$  is equal to 0.117. In other words,  $pmH_1$  in the  $SO_4^=$  containing reference solutions is found equal to 2.085 if one assumes that  $\gamma_{HCl}$  in 0.01 HCl + 0.49 NaCl + 0.030 MgSO<sub>4</sub> + 0.026 MgCl<sub>2</sub> has the same value as that derived from measurements in 0.01 HCl + 0.49 NaCl + 0.056 MgCl<sub>2</sub>. At 1000 kg cm<sup>-2</sup>, with  $K_{HSO_4}^- = 2.26 \ 10^{-2}$ ,  $pmH_{1000} = 2.043$ ; the difference  $pmH_1 - pmH_{1000} = 0.045$  represents equally 80% of the effect of pressure observed in Fig. 8. Further studies on the equilibrium of sulfuric acid will be necessary to verify these estimates, especially since  $-\Delta V_1^\circ$  for SO<sub>4</sub>H<sup>-</sup> is only known from density measurements, with values between 12.0 and 20.6 cm<sup>3</sup> mole<sup>-1</sup> (Hamann, private communication). communication).

If the above corrections were valid, then the values of pk', pk", pmH given in this paper would have to be increased by 0.09 at 1 atm; the calculated values be increased by 0.09 at 1 atm; the calculated values of  $paH_1$  in Table I and the values of  $pK''_{(1)1}$ ,  $pK''_{(2)1}$ remain unchanged whatever the correction;  $\Delta pk'$ ,  $\Delta pk''$ at 1000 kg cm<sup>-2</sup> and the corresponding  $\Delta pH$  would have to be increased by 0.045. These corrections would lead to another coherent set of dissociation functions to calculate the equi-librium of  $H_2CO_3$  in sea water from the corresponding corrected nmH measurements giving evently the same

librium of  $H_2CO_3$  in sea water from the corresponding corrected pmH measurements giving exactly the same results as the set of functions of Table II. Although a precise knowledge of the salt effect of  $SO_4^=$  ions is needed for an approach toward the ab-solute values of  $k_{(1)}$ ,  $k_{(2)}$ , and pmH in sea water, this search is only of academic interest for most of the oceanographic calculations. Finally, it appears that these could best be made from straight forward pwH $= -\log m_{H+\gamma_H+} \gamma_{C1-}$  determinations at any pres-sure (using half-cells without  $SO_4^=$ ) and apparent constants defined as  $K'' \gamma_{C1-} = k'\gamma_{H+} \gamma_{C1-}$ , thus keep-ing the advantages of junctionless cells and eliminat-ing the apparent arbitrariness of the different systems of ionization functions. Sufficient data are given in this paper to make this conversion, since the effect of pressure on  $\gamma_{HC1}$  can easily be calculated in pure HCl [see Harned and Owen (10), p. 507].

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